

1.1 Place Value

- We have a strange way of writing numbers, where the same digit represents a different amount depending on where it comes in the number. When reading long numbers, pupils need to count the columns from the *right* and then read the number from the *left*. Spaces between Th and H, M and HTh, etc., are difficult for many pupils to “see”.
- House prices: The value of a house (a “place” where you live) depends on
 - what it’s like (number of rooms, condition, age, etc.); and
 - where it is (near to shops/schools, quiet neighbourhood, etc.).

Two identical houses in different streets can be worth very different amounts: location matters. Similarly, a number **4** is worth very different amounts in **2478.63** and **36.8742**.

- Why it matters: Being one column out can make a very big difference; e.g.,
 - a nurse giving an injection – is it 0.01 cm^3 or 0.001 cm^3 ? ($10 \times$ difference!)
 - writing a cheque – is it £340.00 or £3400.00? ($10 \times$ difference!)
- Can continue the “houses” analogy by relating place value columns to streets:

M	HTh	TTh	Th	H	T	U	t	h	th	tth
	4	0	0	0	0	0				

M is the “up-market” end of town (where the millionaires live): a number-4-house in M-street is worth ten times as much as a number-4-house in HTh street.

- 1.1.1** Imagine I have just one each of the digits 1, 4 and 5 (could write them on cards to emphasise only one of each).
What different numbers can I make?
How much is the 4 worth in each number?

*Answers: 145, 154, 451, 415, 514, 541; not including decimals (could write them in a systematic order so we know we’ve got them all).
e.g., in 145, value of “4” = $4 \times 10 = 40$*

- 1.1.2** Oral work:
How much is the 4 worth in these numbers?

343	4333	3334.33	33.433	33.34
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Answers: not just “hundreds” but “four hundred”.

40	4000	4 or 4 units	0.4	0.04
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- 1.1.3** Use all the digits 1,2,3,4,5 and 6, once each to make numbers in which the 4 is worth 40 000, 4000, 400, 40, 4, 0.4, 0.04, 0.004.

e.g., 146 532, 364 215, etc.

- 1.1.4** **NEED** newspaper pages containing numbers. Find numbers containing a 4 that is worth these amounts: 40 000, 4000, 400, 40, 4, 0.4, 0.04 and 0.004.

Could be money, numbers of people or anything else. It’s possible to do this with all kinds of newspapers or magazines.

- 1.1.5** Why do we have zero? What’s the point of a number that isn’t worth anything?

The symbol “0” holds place differently in bases other than 10; e.g., in base 2 the number “100” is actually 4.

*Answer: it’s a “place holder” – it shows how much the other digits are worth.
Other cultures have used different number systems (e.g., Roman numerals have no zero). “Zero” wasn’t counted as a “number” until relatively late.*

- 1.1.6** Popeye. Find out what place value has to do with the history of the cartoon character Popeye.

Apparently spinach isn’t quite as good a source of iron as was originally thought. A decimal point in the wrong place gave a false impression in a scientific report!